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Adapting Neural Networks for the Estimation of Treatment Effects

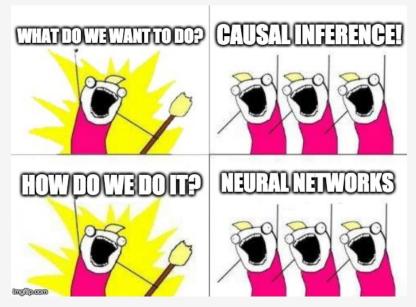
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Causal Inference with Neural Nets using Observational Data



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What is a Causal Question?

Questions about prediction:

- Will I have a headache tomorrow, given that I take this pill?
- What is the rate of drowning death, conditional on the ice cream sales is high?

Questions involve intervention:

- If I take this pill, will I have a headache tomorrow?
- Given that we increase the ice cream sales, what will the rate of drowning death be?

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What is a Causal Question?

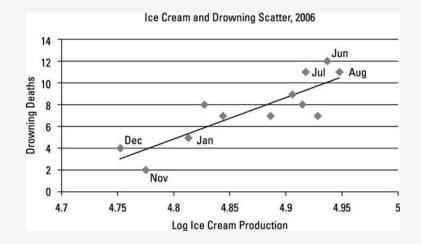
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Observational Data: Confounding is a Problem



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Adapting Neural Networks for the Estimation of Treatment Effects | Overview

RCT Data: Not Accessible



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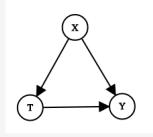
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Causal Inference with Observational Data

Example

- treatment *T* (patient gets a drug)
- outcome Y (whether they recover)
- covariates X (illness severity, socioeconomic status)

What is expected effect of *intervening* by assigning the drug?

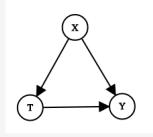


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The average treatment effect is:

$$\psi = \mathbb{E}[Y \mid do(T = 1)] - \mathbb{E}[Y \mid do(T = 0)]$$
$$\psi \neq \mathbb{E}[Y \mid T = 1] - \mathbb{E}[Y \mid T = 0]$$

Theorem (No unobserved contounding) If covariates X "block all backdoor paths" then

$$\psi = \mathbb{E}[Y \mid \operatorname{do}(T=1)] - \mathbb{E}[Y \mid \operatorname{do}(T=0)]$$
$$= \mathbb{E}[\mathbb{E}[Y \mid T=1, X] - \mathbb{E}[Y \mid T=0, X]]$$

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Average Treatment Effect: $\psi = \mathbb{E}[\mathbb{E}[Y \mid T = 1, X] - \mathbb{E}[Y \mid T = 0, X]]$

Back Door Adjustment Let $Q(t,x) = \mathbb{E}[Y \mid t,x]$, here is an estimator: $\hat{\psi}^Q = \frac{1}{n} \sum_i \left[\hat{Q}(1,x_i) - \hat{Q}(0,x_i) \right]$

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Alternatively:

Average Treatment Effect:

$$\psi = \mathbb{E}[\mathbb{E}[Y \mid T = 1, X] - \mathbb{E}[Y \mid T = 0, X]]$$

Inverse Probability of Treatment Weighted Estimator (IPTW) Let g(x) = P(T = 1 | x), here is another estimator $\hat{\psi}^g = \frac{1}{n} \sum_i \left(\frac{t_i}{\hat{g}(x_i)} - \frac{1 - t_i}{1 - \hat{g}(x_i)} \right) y_i$

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Models

expected outcome:
$$Q(t,x) = \mathbb{E}[Y | t,x]$$

propensity score: $g(x) = P(T = 1 | x)$
ATE: $\psi = \mathbb{E}[\mathbb{E}[Y | T = 1,X] - \mathbb{E}[Y | T = 0,X]]$

Semi-parametric efficient

- More complicated $\hat{\psi}$ use both \hat{Q} and \hat{g}
- Nice asymptotic properties: low bias / efficient

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Example: A Semi-parametric Efficient Estimator

Augmented IPTW $\hat{\psi} = \hat{Q}(1,x) - \hat{Q}(0,x) + \left(\frac{t}{\hat{g}(x)} - \frac{1-t}{1-\hat{g}(x)}\right) \left\{y - \hat{Q}(t,x)\right\}$

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We want to use neural networks to model Q and g.

How should we adapt the design and training of these networks so that $\hat{\psi}$ is a good estimate of ψ ?

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Adaptations

- A neural network architecture—the Dragonnet—based on the sufficiency of the propensity score for causal estimation.
- A regularization procedure—targeted regularization—based on non-parametric estimation theory.

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Dragonnet

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Highlight

If the average treatment effect ψ is identifiable from observational data by adjusting for X, then adjusting for the propensity score also suffices.

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Theorem (Rosenbaum and Rubin 1983)
If
$$\psi = \mathbb{E}[\mathbb{E}[Y \mid T = 1, X] - \mathbb{E}[Y \mid T = 0, X]]$$
, then
 $\psi = \mathbb{E}[\mathbb{E}[Y \mid T = 1, g(X)] - \mathbb{E}[Y \mid T = 0, g(X)]]$

 \Rightarrow estimate $\hat{Q}(t,x)$ using only parts of X relevant for ${\mathcal T}$

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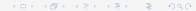
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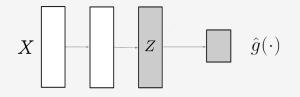
Goal

Estimate $\hat{Q}(t,x)$ using only parts of X relevant for T



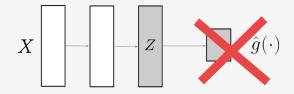


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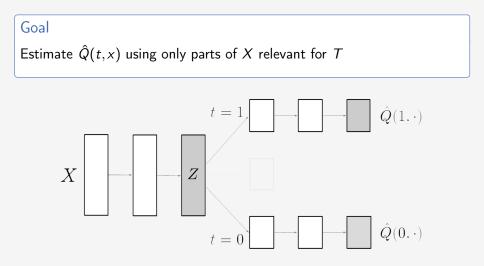


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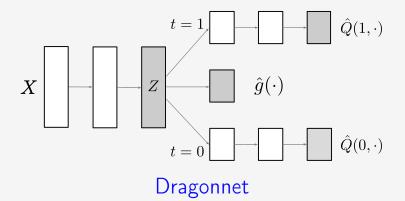
Better: Dragonnet

Goal: Estimate $\hat{Q}(t,x)$ using only parts of X relevant for T Downstream estimator: $\hat{\psi}^Q = \frac{1}{n} \sum_i \left[\hat{Q}(1,x_i) - \hat{Q}(0,x_i) \right]$

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Is the End-to-end model better?

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Is the End-to-end model better?

 Table 4: Dragonnet produces more accurate estimates than NEDnet, a multi-stage alternative. Table entries are mean absolute error over all datasets.

IHDP	$\hat{\psi}^{\mathbf{Q}}$	$\hat{\psi}^{\mathrm{TMLE}}$	ACIC	$\hat{\psi}^{\mathbf{Q}}$	$\hat{\psi}^{\mathrm{TMLE}}$
Dragonnet NEDnet	$\begin{array}{c} 0.12 \pm 0.00 \\ 0.15 \pm 0.01 \end{array}$		Dragonnet NEDnet	$0.55 \\ 1.49$	$1.97 \\ 2.80$

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Does Dragonnet Actually Use Propensity Score Sufficiency?

TARNET ¹= Dragonnet without treatment head

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$$\hat{\psi}^Q = \frac{1}{n} \sum_i \left[\hat{Q}(1, x_i) - \hat{Q}(0, x_i) \right]$$

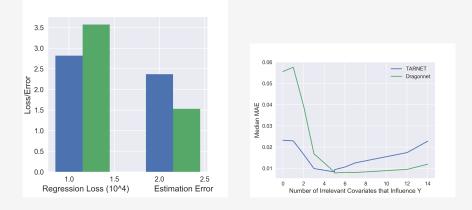
¹https://arxiv.org/abs/1606.03976

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Targeted Regularization

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Recall:

expected outcome: $Q(t,x) = \mathbb{E}[Y | t,x]$ propensity score: g(x) = P(T = 1 | x)Average treatment effect: $\psi = \mathbb{E}[\mathbb{E}[Y | T = 1, X] - \mathbb{E}[Y | T = 0, X]]$

Semi-parametric efficient

- More complicated $\hat{\psi}$ use both \hat{Q} and \hat{g}
- Nice asymptotic properties: low bias / efficient

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Asymptotics

If $(\hat{Q}, \hat{g}, \hat{\psi})$ satisify a certain equation, then

robustness in the double machine-learning sense--- $\hat{\psi}$ converges to ψ at a fast rate even if \hat{Q} and \hat{g} converge slowly

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efficiency---asymptotically, $\hat{\psi}$ has the lowest variance of any consistent estimator of ψ

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 \blacksquare efficiency---asymptotically, $\hat{\psi}$ has the lowest variance of any consistent estimator of ψ

Asymptotics hold if

- **1** \hat{Q} and \hat{g} are consistent
- **2** $(\hat{Q}, \hat{g}, \hat{\psi})$ satisfy non-parametric estimating equation,

$$0=\frac{1}{n}\sum_{i}\varphi(y_{i},t_{i},x_{i};\hat{Q},\hat{g},\hat{\psi}),$$

where

$$\varphi(y,t,x;Q,g,\psi) = Q(1,x) - Q(0,x) + \left(\frac{t}{g(x)} - \frac{1-t}{1-g(x)}\right) \{y - Q(t,x)\} - \psi$$

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A-IPTW

1 Obvious: fit \hat{Q} and \hat{g} , then choose $\hat{\psi}$ so non-parametric estimating equation is satisfied

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$$\hat{\psi}^Q = \frac{1}{n} \sum_i \left[\hat{Q}(1, x_i) - \hat{Q}(0, x_i) \right]$$
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Fit \hat{Q} and \hat{g} so non-parametric estimating equation is satisfied

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Fit \hat{Q} and \hat{g} so non-parametric estimating equation is satisfied

Introduce extra parameter $\boldsymbol{\varepsilon}$ and regularization term $\gamma(y, t, x; \theta, \boldsymbol{\varepsilon})$

$$\tilde{Q}(t_i, x_i; \theta, \varepsilon) = Q^{\mathrm{nn}}(t_i, x_i; \theta) + \varepsilon \Big[\frac{t_i}{g^{\mathrm{nn}}(x_i; \theta)} - \frac{1 - t_i}{1 - g^{\mathrm{nn}}(x_i; \theta)} \Big]$$
$$\gamma(y_i, t_i, x_i; \theta, \varepsilon) = (y_i - \tilde{Q}(t_i, x_i; \theta, \varepsilon))^2$$

Then train as

$$\hat{\theta}, \hat{\varepsilon} = \underset{\theta, \varepsilon}{\operatorname{argmin}} \left[\underbrace{\hat{\mathcal{R}}(\theta; \boldsymbol{X})}_{\text{usual objective}} + \alpha \underbrace{\frac{1}{n} \sum_{i} \gamma(y_i, t_i, x_i; \theta, \varepsilon)}_{\text{targeted regularization}} \right]$$

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Payoff

Define an estimator $\hat{\psi}^{\mathrm{treg}}$,

$$\hat{\psi}^{\text{treg}} = rac{1}{n} \sum_{i} \hat{Q}^{\text{treg}}(1, x_i) - \hat{Q}^{\text{treg}}(0, x_i), \quad \text{where}$$

 $\hat{Q}^{\text{treg}} = \tilde{Q}(\cdot, \cdot; \hat{\theta}, \hat{\varepsilon}).$

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Payoff

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 $\hat{Q}^{\text{treg}} = \tilde{Q}(\cdot, \cdot; \hat{\theta}, \hat{\varepsilon}).$

The point is:

$$0 = \partial_{\varepsilon} \big(\hat{R}(\theta; \boldsymbol{X}) + \alpha \frac{1}{n} \sum_{i} \gamma(y_{i}, t_{i}, x_{i}; \theta, \varepsilon) \big) |_{\hat{\varepsilon}} = \alpha \frac{1}{n} \sum \varphi(y_{i}, t_{i}, x_{i}; \hat{Q}^{\text{treg}}, \hat{g}, \hat{\psi}^{\text{treg}}).$$

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Payoff

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$$\hat{\psi}^{\text{treg}} = rac{1}{n} \sum_{i} \hat{Q}^{\text{treg}}(1, x_i) - \hat{Q}^{\text{treg}}(0, x_i), \quad \text{where}$$

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The point is:

$$0 = \partial_{\varepsilon} \big(\hat{R}(\theta; \boldsymbol{X}) + \alpha \frac{1}{n} \sum_{i} \gamma(y_{i}, t_{i}, x_{i}; \theta, \varepsilon) \big) |_{\hat{\varepsilon}} = \alpha \frac{1}{n} \sum \varphi(y_{i}, t_{i}, x_{i}; \hat{Q}^{\text{treg}}, \hat{g}, \hat{\psi}^{\text{treg}}).$$

That is, minimizing the targeted regularization term forces $(\hat{Q}^{\text{treg}}, \hat{g}, \hat{\psi}^{\text{treg}})$ to satisfy the non-parametric estimating equation.

Experiment

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Infant Health Development Program Benchmark (IHDP)

Method	Δ_{in}	Δ_{out}	Δ_{all}
BNN [JSS16]	$0.37 \pm .03$	$0.42\pm.03$	_
TARNET [SJS16]	$0.26\pm.01$	$0.28\pm.01$	_
CFR Wass[SJS16]	$0.25\pm.01$	$0.27\pm.01$	
CEVAEs [Lou+17]	$0.34\pm.01$	$0.46\pm.02$	
GANITE [YJS18]	$0.43 \pm .05$	$0.49\pm.05$	_
baseline (TARNET)	$0.16\pm.01$	$0.21\pm.01$	$0.13 \pm .00$
baseline + t-reg	$0.15\pm.01$	$0.20\pm.01$	$0.12\pm.00$
Dragonnet	$0.14\pm.01$	$0.21\pm.01$	$0.12\pm.00$
Dragonnet + t-reg	$0.14\pm.01$	$0.20\pm.01$	$0.11 \pm .00$

 Table 2: Dragonnet and targeted regularization improve estimation on average on ACIC 2018. Table entries are mean absolute error over all datasets.

 Table 3: Dragonnet and targeted regularization improve over the baseline about half the time, but improvement is substantial when it does happen. Error values are mean absolute error on ACIC 2018.

Method	Δ_{all}
baseline (TARNET)	1.45
baseline + t-reg	1.40
Dragonnet	0.55
Dragonnet + t-reg	0.35

ψ^Q	$\%_{improve}$	\uparrow_{avg}	\downarrow_{avg}
baseline:	0%	0	0
+ t-reg	42%	0.30	0.11
+ dragon	63%	1.42	0.01
+ dragon & t-reg	46%	2.37	0.01

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Summary

 Dragonnet: a neural network architecture based on the sufficiency of the propensity score for causal estimation.

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- targeted regularization: a regularization procedure based on non-parametric estimation theory.
- They both work!

Adapting Neural Networks for the Estimation of Treatment Effects. arxiv:1906.02120

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